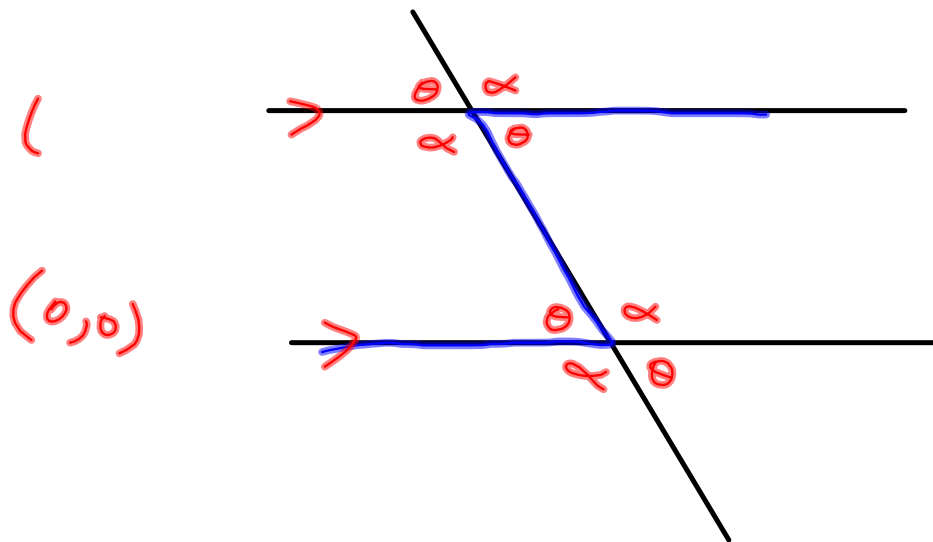
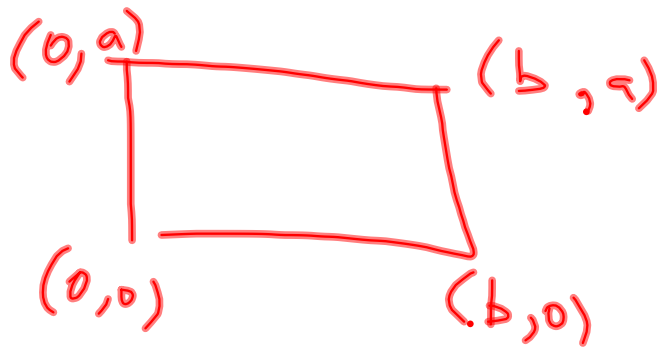
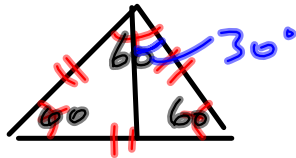


$$\alpha + \theta = 180^\circ$$





regular polygon  
equilateral triangle.

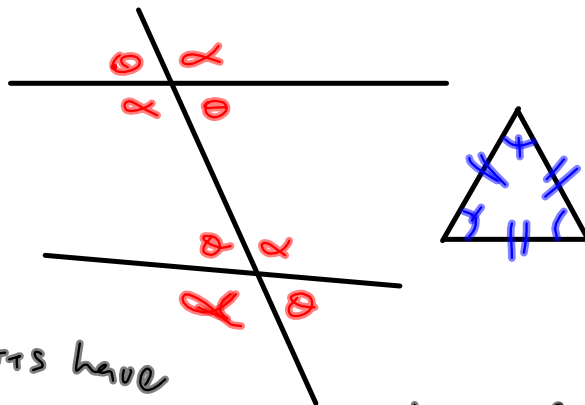
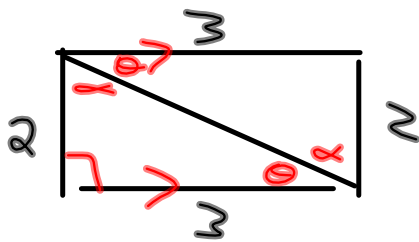


## Unit 14: Solving Geometry

SOH CAH TOA Problems

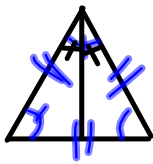
$$c^2 = a^2 + b^2$$

$$\theta + \alpha = 180$$

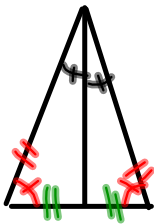
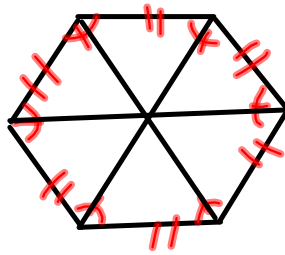


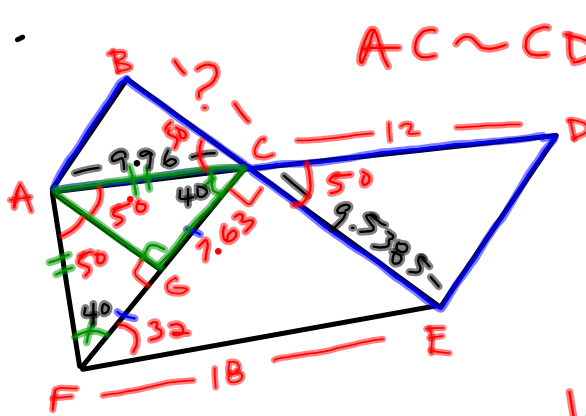
- equivalent 2D figures have same area.
- equivalent 3D figures have same volumes.

# Regular Polygon



regular hexagon

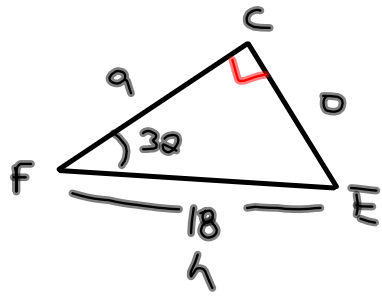




$AC \sim CD$  what's k?

$\Delta ABC \sim \Delta CDE$  similar  
 $\Delta ACF$  is isosceles  
 $\angle FAC = 50^\circ$   
 $\angle CFE = 32^\circ$

What's BC



$\sin \theta = \frac{b}{h}$

$\cos \theta = \frac{a}{h}$

$18 \cdot \sin 32 = \left(\frac{0}{18}\right)$  (crossed out)

$\cos 32 = \frac{a}{18}$

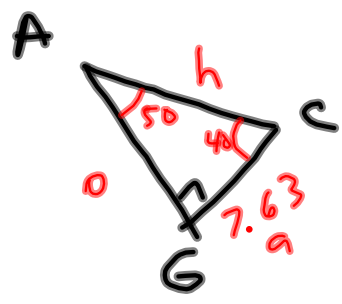
$CE : 0 = 18 \cdot \sin 32$

$a = 18 \cos 32$

$CE : 0 = 9.5385$

$FC : a = 15.2648$

$GC : \frac{a}{2} = 7.63$



$\cos \theta = \frac{a}{h}$

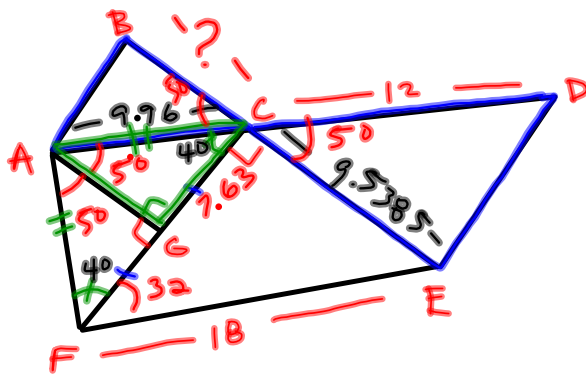
$\cos 40 = \frac{7.63}{h}$

$\frac{h \cos 40}{\cos 40} = \frac{7.63}{\cos 40}$

$h = 9.96$

For similar  $\Delta$ 's

$$k = \frac{\text{Side length of Big } \Delta}{\text{Side length of the corresponding Side of small } \Delta.}$$



$$k = \frac{\text{Big}}{\text{Small}}$$

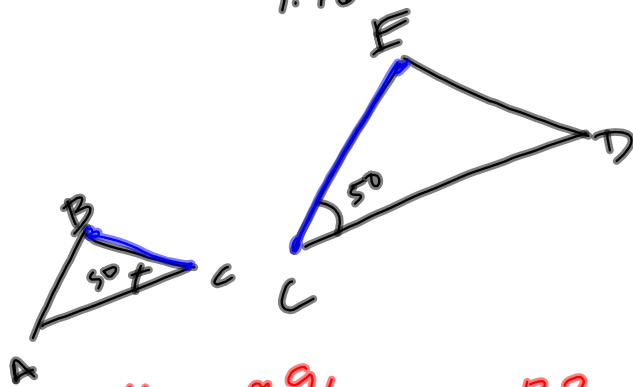
$$k = \frac{12}{9.96} = 1.204$$

$$k = \frac{CE}{BC}$$

$$1.204 = \frac{9.5385}{BC}$$

$$\frac{BC \cdot 1.204}{1.204} = \frac{9.5385}{1.204}$$

$$BC = 7.92$$



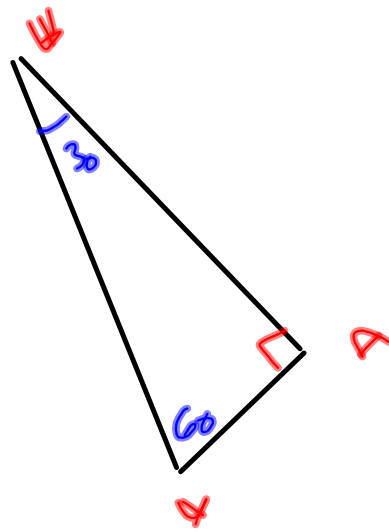
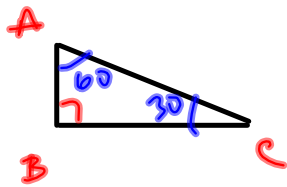
$$k = \frac{\text{small}}{\text{big}} = \frac{9.96}{12} = 0.83$$

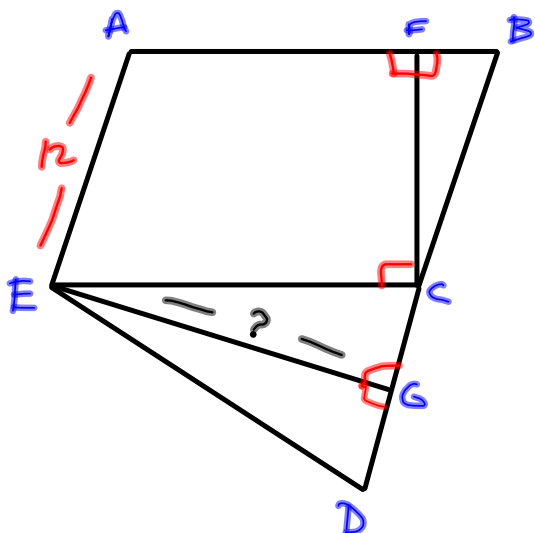
$$k = \frac{BC}{CE} \Rightarrow 0.83 = \frac{BC}{9.5385}$$

$$BC = 0.83 \cdot 9.5385$$

$$k = 7.92$$







$ABCE$  is a parallelogram

$\triangle BCF$  is congruent  
to  $\triangle EDG$

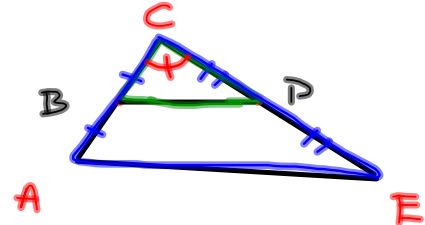
$$\angle DEG = 27^\circ$$

$$\overline{AE} = 12$$

What's the length of  
 $EG$ ?

Recall: Prove that when you join the midpoints of any 2 sides in a triangle, you form a similar  $\Delta$ .

Hypothesis



$CD = DE$   
 $CB = BA$

Conclusion: Prove:  $\frac{A}{A} = \frac{\text{Side B}}{\text{Side B}} = \frac{\text{Side C}}{\text{Side C}}$

Statements  
 $\angle BCD = \angle ACE$   
 $\frac{BC}{AC} = \frac{BC}{AB+BC} = \frac{BC}{BC+BC}$   
 $\frac{BC}{2BC} = \frac{1}{2}$

Justification  
 shared angle  
 hypothesis  
 simplifying

$\frac{CD}{CE} = \frac{CD}{CD+DE} = \frac{CD}{CD+CD}$   
 $= \frac{CD}{2CD} = \frac{1}{2}$

hypothesis  
 simplifying

$\therefore \Delta BCD \sim \Delta ACE$

$A=A \quad \frac{S}{S} = \frac{S}{S} \quad \checkmark$   
 $\square$

Congruent

•  $SAS = SAS$

•  $SSS = SSS$

•  $ASA = ASA$

Similar

•  $\frac{S_{Big}}{S_{Small}} = \frac{S_{Big}}{S_{Small}} \quad A = A$

•  $\frac{S_{Big}}{S_{Small}} = \frac{S_{Big}}{S_{Small}} = \frac{S_{Big}}{S_{Small}}$

•  $\checkmark \checkmark A = \checkmark \checkmark A$

