

Lesson 7: Representations of 3D solids using Projections (5 different types) April 5th, 2024

definition: projection - a drawing of a 3D object (solid) on a 2D plane (i.e. a piece of paper)

• 2 types of Central Projections

#1. Perspective w̄ one Vanishing Point.

e.x. Pg 62

Here is a reproduction of a painting from the 15th century that has long been credited to Italian painter Piero della Francesca and entitled *Ideal City*. Thanks to his rigorous use of perspective, he was able to achieve a remarkable illusion of depth.



Figure 2.3

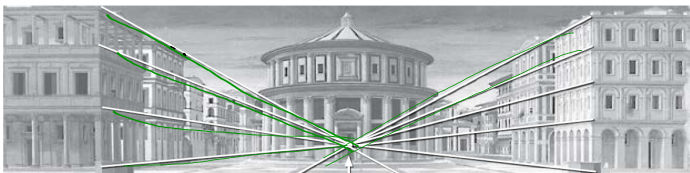
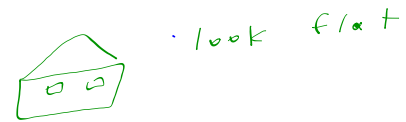


Figure 2.8

Vanishing Point



↪ illusion of depth.

How?

↪ all vertical lines are parallel

↪ some horizontal lines are parallel (in the drawing)

↪ horizontal lines on non-front face of solid are not parallel in drawing (even tho parallel in reality)

Terminology :

1.1 Perspective With One Vanishing Point

Horizon line

vanishing point

vanishing lines

vertical lines is parallel to

$\overline{AX} \parallel \overline{By}$

$\overline{By} \parallel \overline{CZ}$

line segment

horizontal lines

$\overline{AB} \parallel \overline{xy}$

$\overline{CD} \parallel \overline{AB}$

BUT!

$\overline{BC} \not\parallel \overline{yz}$

(no in reality $\overline{BC} \parallel \overline{yz}$)

1.1.1 Example

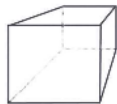
Determine the vanishing point and horizon line for the following prism:

v. point

the horizon

1.1.2 Practice

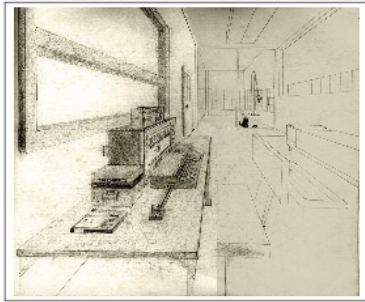
Determine the vanishing point and horizon line for the following prism:



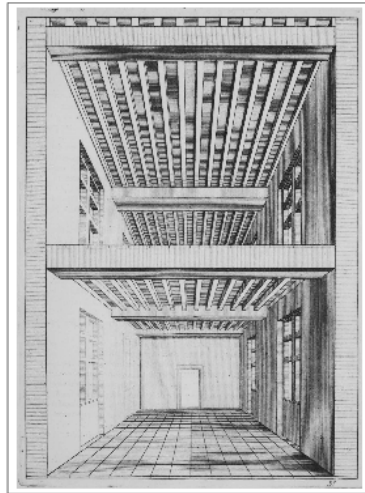
1.1.3 Practice

For each of the following images, determine the vanishing point and horizon line:

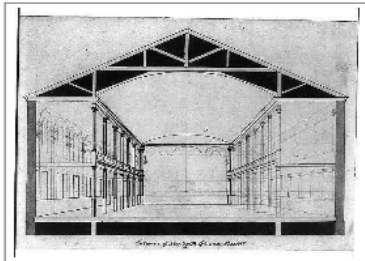
#1



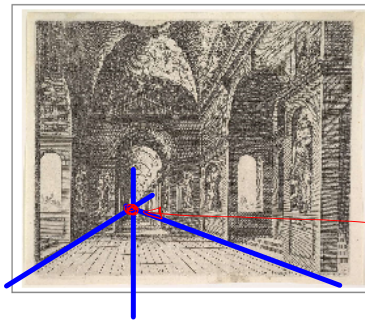
#2



#3



#4

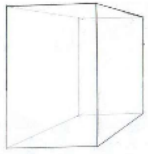


vanishing point
which our eyes are
drawn to.

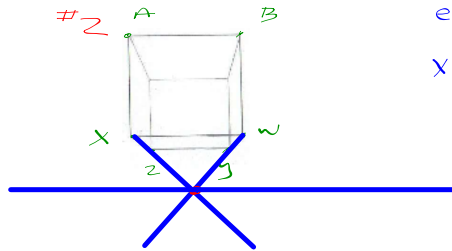
1.1.4 Practice

For each of the following drawings, determine the vanishing point and horizon line:

#1



#2

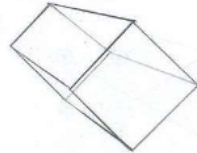


extend
 \bar{x} and \bar{y}

#3



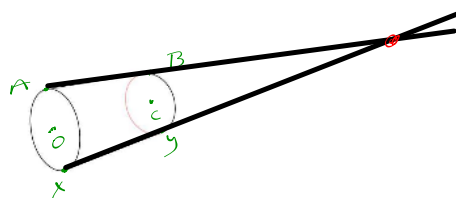
#4



#5



#6

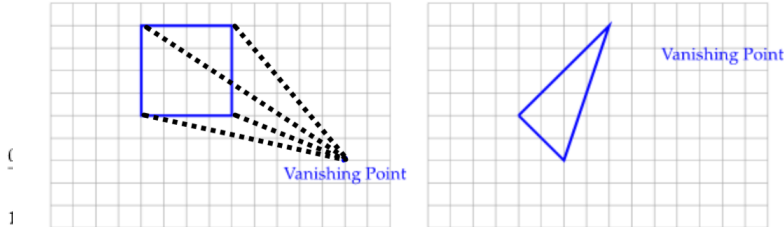


extend
 \bar{AB} \bar{xy}

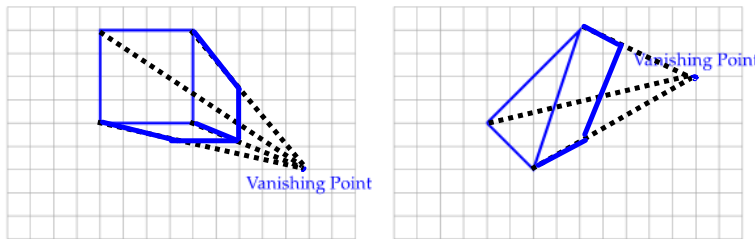
Drawing the 3D solid on the 2D \bar{w} Central Proj. \bar{w} one v. point

1.1.5 Example

Complete the drawing of the following prisms with one perspective point (the depth of the prism in this case is up to you, there are many possibilities).

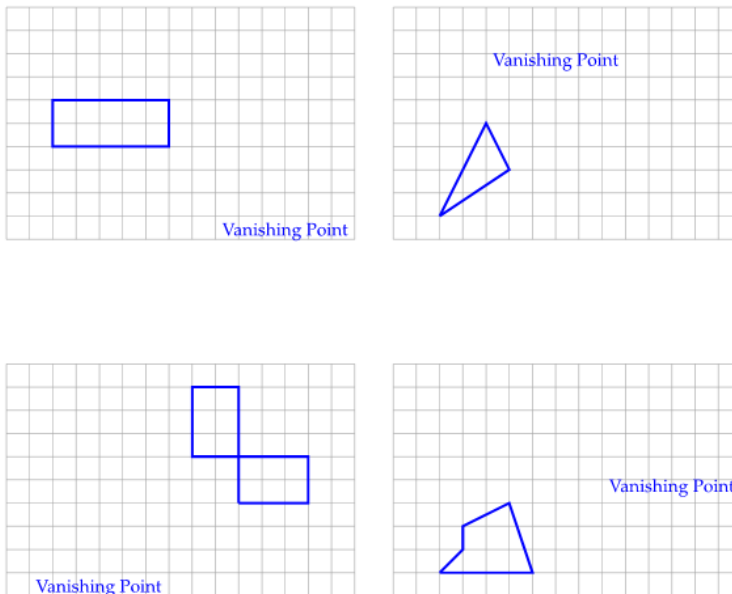


Complete the drawing of the following prisms with one perspective point (the depth of the prism in this case is up to you, there are many possibilities).



1.1.6 Practice

Complete the drawing of the following prisms with one perspective point (the depth of the prism in this case is up to you, there are many possibilities).



step i (done)
 • draw front face un-distorted.
 • pick v. point (where you want eye level)

step ii • from each vertex of face draw dotted v. lines to v. point.

step iii • Draw a (vertical) line parallel to front face limited to correct plane.

step iv • connect the vertices

You do

2nd Central Projection

A perspective with 2 vanishing points

1 v. point!



Figure 2.4

- straight on front view
- front facade/face is \parallel to drawing

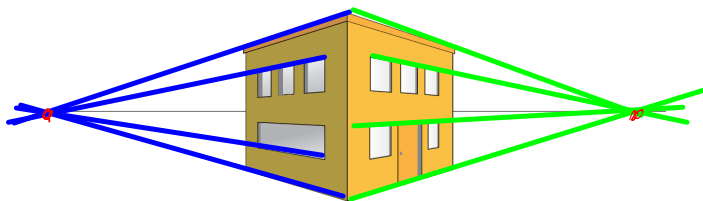
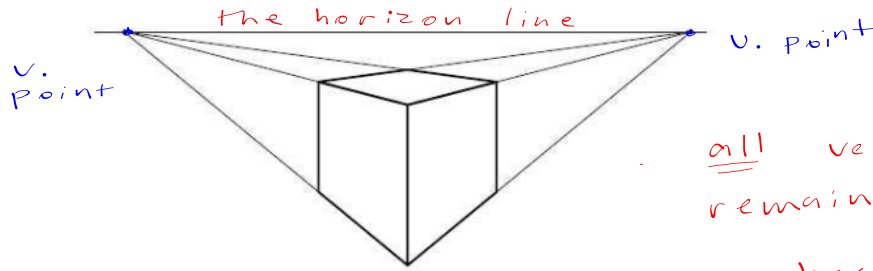


Figure 2.5

2 vanishing points!
 What's the difference?
 (pg 67 recaps the difference)
 → no face of solid is \parallel to drawing.

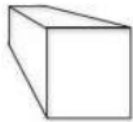
Perspective with Two Vanishing Points This perspective has two vanishing points.



- all vertical line remain parallel
- no horizontal line is parallel

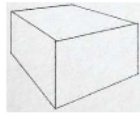
1.2.1 Example

Determine whether the following prisms have one or two vanishing points:



1.2.2 Example

Determine the two vanishing points and horizon for the following object:

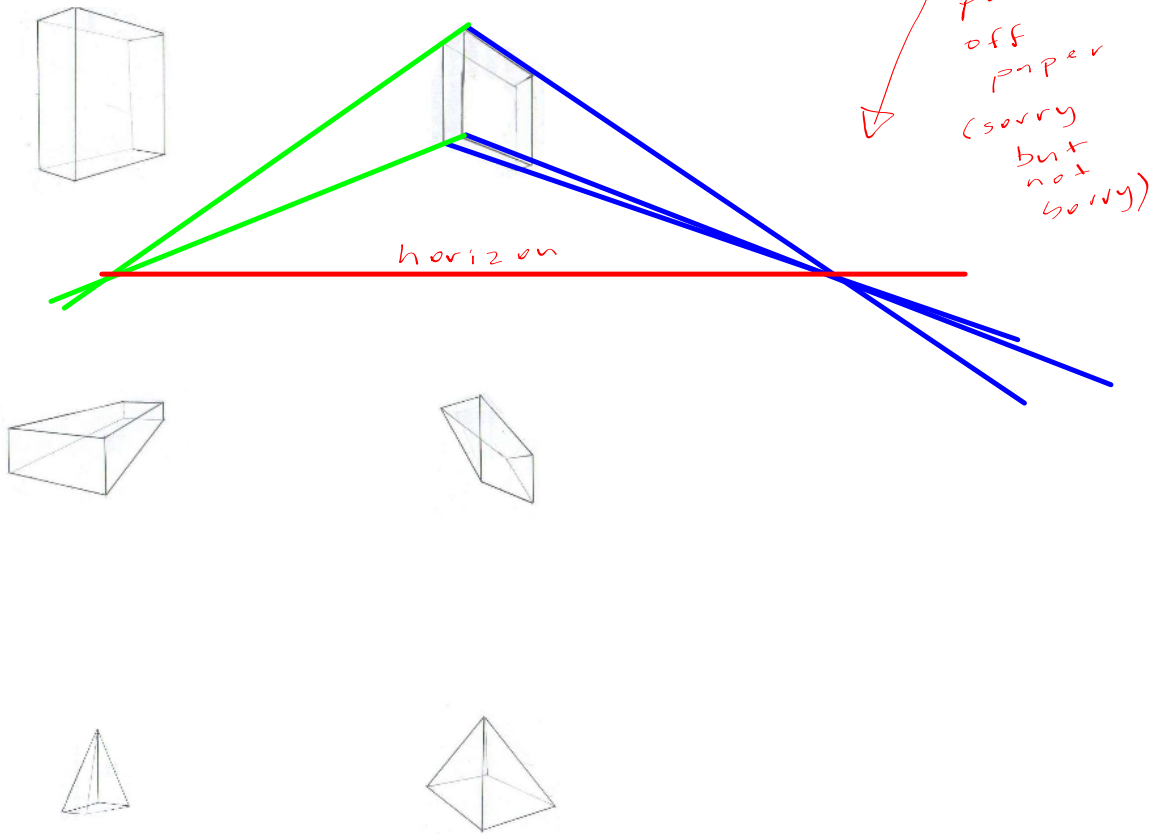


note: the horizon line must go thru both v. points.

you do and pg 8!

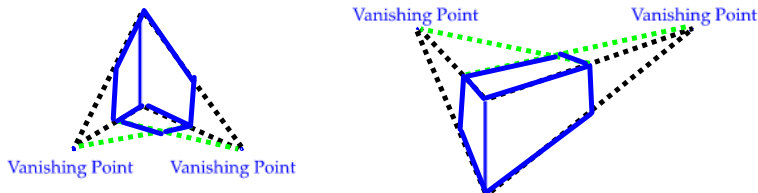
1.2.3 Practice

For each of the following drawings, determine the vanishing points and horizon line:



1.2.4 Example

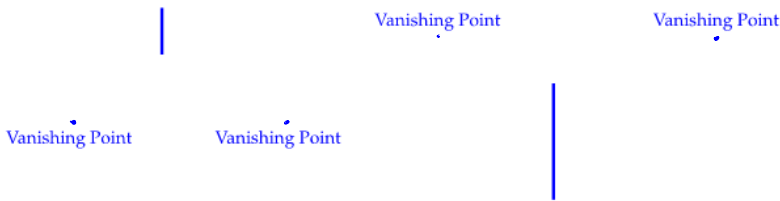
Draw rectangular prisms with two vanishing points (the depth is up to you!):



1.2.5 Practice

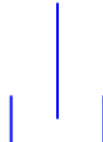
You do the next three!

Draw rectangular prisms with two vanishing points (the depth is up to you!):



1.2.6 Practice

The following is a triangular prism with two vanishing points. Complete the drawing by first identifying the vanishing points and horizon line.



Step i (done)

one vertical line, and 2 v. points.

Step ii draw

dotted lines from endpoints of line to each v. point.

Step iii. Draw other 11 vertical line with the dots

Step iv. connect the endpoints of new vertical line to v. point.

Step v. connect vertices

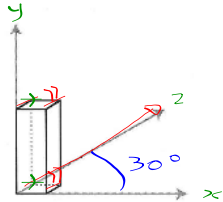
5 projections in total

2 Parallel Projections — 2 types — All vertical AND horizontal line remain || in drawing.

In parallel projections, the parallel dimensions of the object remain parallel in their projected form.

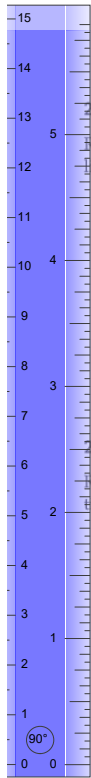
1st type:

2.1 Cavalier (Oblique) Projection



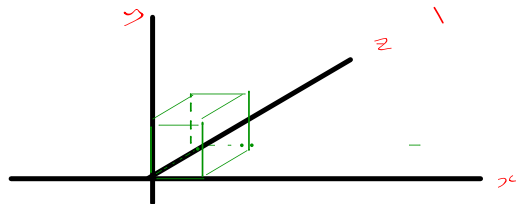
Conventions:

- The depth axis forms a 30° or 45° angle with the horizontal. *↳ good w graph paper*
- The receding edges are reduced in size by approximately 50% or 60% }
- The non-visible edges of the prism are drawn with dotted lines.



2.1.1 Example

Represent a rectangular prism whose real dimensions measure 1cm x 1cm x 2cm (depth) in cavalier (oblique) perspective:



stays the same since in the front face

must be reduced
2cm = 1cm (50%)
Pre-step reduce depth measure by 50%

- step i: make axis
- step ii: draw the front 2D face according to measures (not depth) (from origin)
- step iii: draw the depth line segments @ reduced measure || to depth axis.
- step iv: connect vertices

2.1.2 Practice

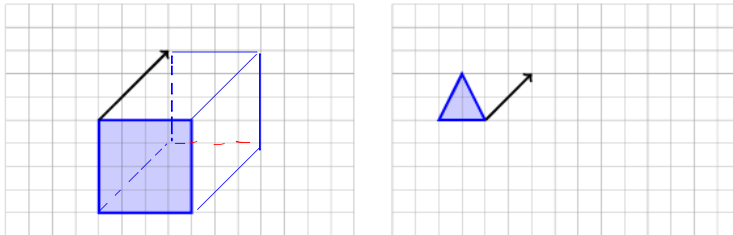
Represent a cube whose real dimensions measure 2cm x 2cm x 2cm in cavalier (oblique) perspective

• You do →
• Bonus: start pg 11

2.1.3 Example: Oblique Perspective as a Translation

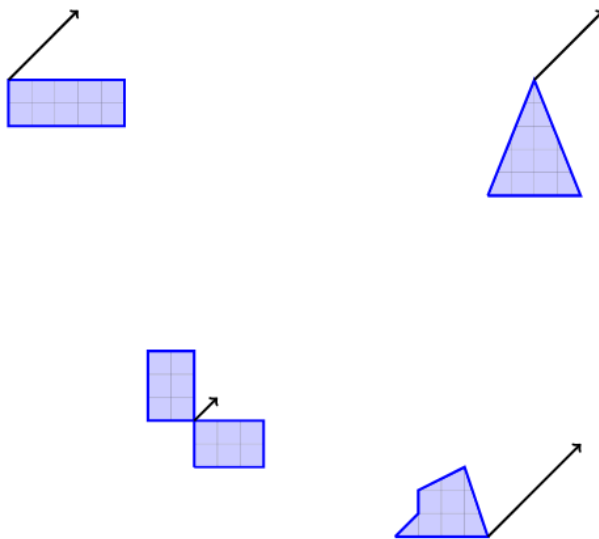
We can also obtain an oblique projection by translating a polygon in a grid. The translation arrow (vector) is usually 45° in a given direction.

Complete the drawing of the following oblique projections, given the translation arrow:



2.1.4 Practice

Complete the drawing of the following oblique projections, given the translation arrow:



ex. 1. Draw a rectangular prism that's $2\text{cm} \times 2\text{cm} \times 4\text{cm}$.

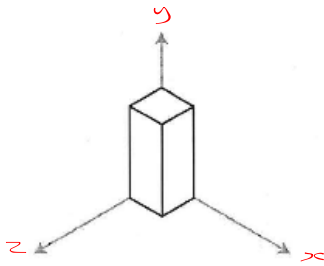
pre steps: divide the depth dimension by 2 (50% reduction)

$$2\text{cm} \times 2\text{cm} \times \frac{4}{2} = 2\text{cm}$$

ex 2 Draw a cube by $2\text{cm} \times 2\text{cm} \times 2\text{cm}$

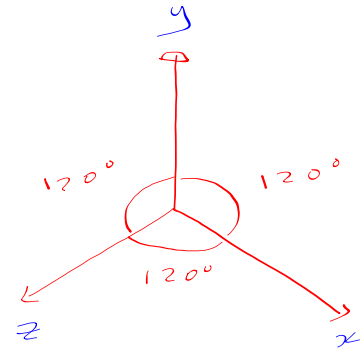
$$2\text{cm} \times 2\text{cm} \times \frac{2}{2} = 1\text{cm}$$

2nd type of Parallel Projection



Conventions:

- The axes meet at 120° angles.
- All the segments that are congruent in reality and that are parallel to one of the axes remain congruent in the representation.

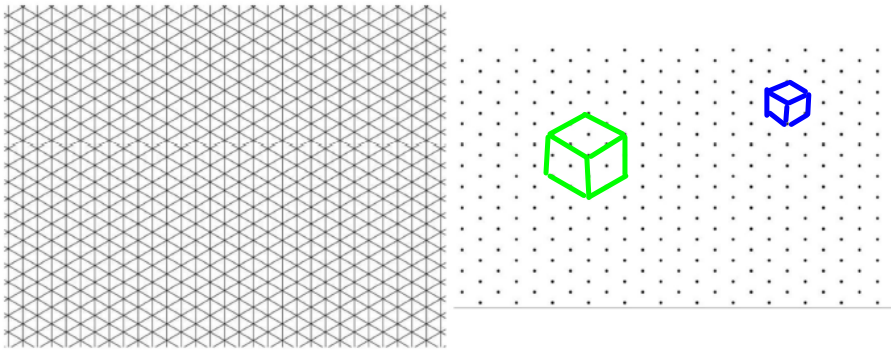


2.2 Parallel Isometric (Axonometric) Projection

Isometric projections are parallel projections in which congruent dimensions of the original object remain congruent in the representation. / drawings.

2.2.3 Example: Using Isometric Grid Paper/Dots

Isometric projections are easier to draw when using isometric grids. There are two types (see below):



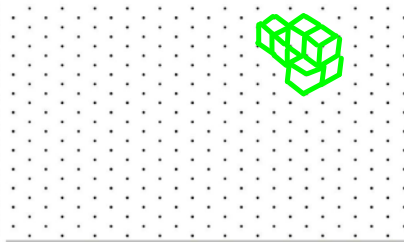
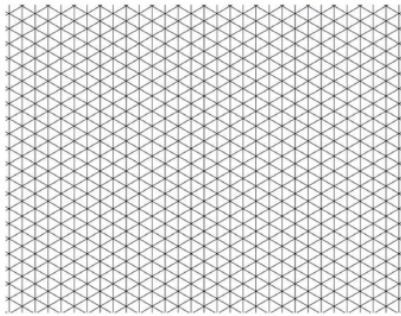
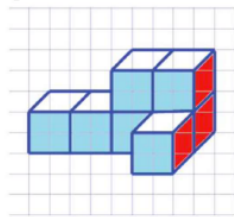
Q: How would you draw a cube using either grid? Draw a cube in each grid above.

TIPS:

- use a pencil
- start @ top.
- don't do back dotted edges

2.2.4 Practice

Reproduce the following oblique representation in isometric representation in each grid below:

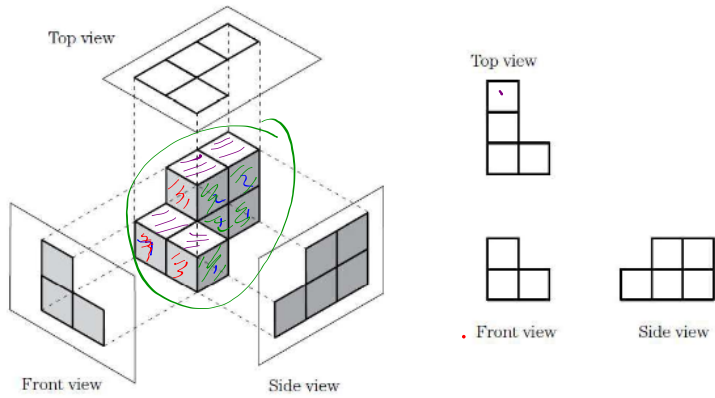


- TIPS:
- use a pencil
 - start @ top.
 - don't do back dotted edges

pg 14

3 Orthogonal Projection

With Orthogonal projections, we actually project a 3D object onto a 2D plane



3.1 Example

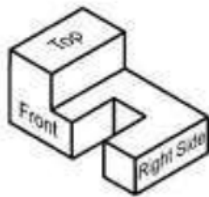
Represent the top, front and side view of the following object:

The 3D object is a stack of cubes. The front view is a 3x2 grid with a 3x1 grid on top of the left column. The side view is a 3x1 grid with a 2x1 grid on top of the left column. The top view is a 3x2 grid with a 2x1 grid on top of the left column. The 2D projections are drawn on a grid. The side view is green, the front view is red, and the top view is blue. A red 'X' is drawn next to the top view.

You do
3.1.2
New stuff @
2pm.

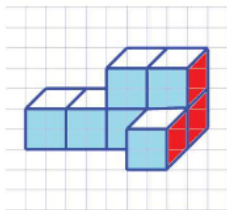
3.1.1 Practice

Represent the top, front and side view of the following object:



3.1.2 Practice

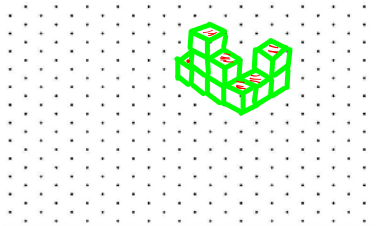
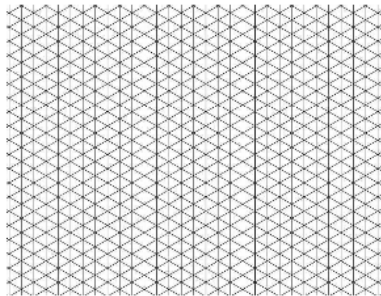
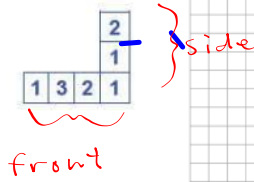
Represent the top, front and side view of the following object:



3.1.3 Example: Drawing from Coded Blue Print

Represent the front and side view of the object with the following coded blue print as well as the entire object in cavalier(oblique) projection and isometric projection:

rep. the
of cubes



Pg 16

You try on
Pg 17
and show me
other drawings.

- HMWK:
- pg 68
- pg 69 #2.8 a)-c)
- pg 77
- pg 78 (not #2.15)
- pg 83
- pg 85
- (answer key for last examples that you'll practice will be uploaded to teams)