

## Real Functions and Equations

### Constant Function (zeroth degree):

$$y = k$$

$(0, k)$  is the y-intercept

### Linear Function (first degree):

$$y = ax + k$$

$a$  is the slope,  $(0, k)$  is the y-intercept

### Quadratic Function (second degree):

$$y = ax^2 + bx + c \dots\dots\dots \text{General Form}$$

$$y = a(x - x_1)(x - x_2) \dots\dots \text{X-intercept Form}$$

$$y = a(b(x - h))^2 + k \dots\dots \text{Standard Form}$$

$(h, k)$  is the Vertex

### Absolute Value Function:

$$y = a|b(x - h)| + k \dots\dots\dots \text{Standard Form}$$

$(h, k)$  is the Vertex

### Greatest Integer Function:

$$y = a[b(x - h)] + k \dots\dots\dots \text{Standard Form}$$

$(h, k)$  is a solid point

$$L = \frac{1}{|b|} \dots\dots \text{Step length}$$

If  $b > 0$  then the step is open on the right, closed on the left

If  $b < 0$  then the step is closed on the right, open on the left

$$D = |a| \dots\dots \text{Vertical distance between steps}$$

$$m = ab \dots\dots \text{Slope of the graph}$$

**Rational Function:**

$$y = \frac{a}{b(x-h)} + k \text{ ..... Standard Form}$$

$$x = h, y = k \text{ ..... Asymptotes}$$

**Square-Root Function:**

$$y = a\sqrt{b(x-h)} + k \text{ ..... Standard Form}$$

$(h, k)$  is the Vertex

$b(x-h) \geq 0$  is the Domain

## Quadratic Functions

$$y = ax^2 + bx + c$$

General Form

$$\Delta = b^2 - 4ac$$

Discriminant

$$x = \frac{-b \pm \sqrt{\Delta}}{2a}$$

Quadratic Formula

$$V\left(\frac{-b}{2a}, \frac{-\Delta}{4a}\right)$$

Vertex formula

$$(0, c)$$

Y-intercept

$$x = \frac{-b}{2a}$$

Axis of Symmetry

$$y = a(x - x_1)(x - x_2)$$

X-intercept form

Where  $x_1$  and  $x_2$  are the x-intercepts of the graph.

$$y = a(x - h)^2 + k$$

Standard Equation

$$V(h, k)$$

## Exponential Functions

$$f(x) = ac^{b(x-h)} + k$$

Asymptote:  $y = k$

## Logarithmic Functions

$$f(x) = a \log_c b(x-h) + k$$

Asymptote:  $x = h$

## Logarithmic Laws

1.  $\log_c c = 1$
2.  $\log_c 1 = 0$
3.  $\log_c c^n = n$
4.  $\log_c M + \log_c N = \log_c (M \times N)$
5.  $\log_c M - \log_c N = \log_c \left(\frac{M}{N}\right)$
6.  $\log_c M^n = n \log_c M$
7.  $\log_{1/c} M = -\log_c M$
8.  $\log_c M = \frac{\log M}{\log c}$

## Exponential Expression to Logarithmic Expression

$$y = a^x \leftrightarrow \log_a y = x$$

## Theorems

$$\text{if } c^x = c^y, \text{ then } x = y$$

$$\text{if } a^x = b^y, \text{ then } \log a^x = \log b^y$$

## Exponential Growth and Decay

$$A(t) = A_0 \left(1 + \frac{r}{k}\right)^{kt}$$

$A(t)$  = Amount after  $t$  time

$A_0$  = Initial Amount

$r$  = Rate, expressed as a decimal

$k$  = Compounding Constant

$$A(t) = ac^{kt}$$

$a$  = initial amount

$c$  = rate of change

$k$  = rate constant

$A(t)$  = amount after  $t$  time

## Exponents and Radicals

### Laws of Exponents

$$1. a^m \times a^n = a^{(m+n)}$$

$$2. \frac{a^m}{a^n} = a^{(m-n)}$$

$$3. a^{-n} = \frac{1}{a^n}$$

$$4. a^0 = 1$$

$$5. (a^n)^m = a^{n \times m}$$

$$6. (abc)^n = a^n b^n c^n$$

$$7. \left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

### Radicals to Exponents

$$\sqrt[n]{a^m} = a^{\frac{m}{n}}$$

### Laws of Radicals

$$1. \sqrt{a \times b} = \sqrt{a} \times \sqrt{b}$$

$$2. r\sqrt{a} \times s\sqrt{b} = (r \times s)\sqrt{a \times b}$$

$$3. \sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

$$4. \frac{r\sqrt{a}}{s\sqrt{b}} = \frac{r}{s} \sqrt{\frac{a}{b}}$$

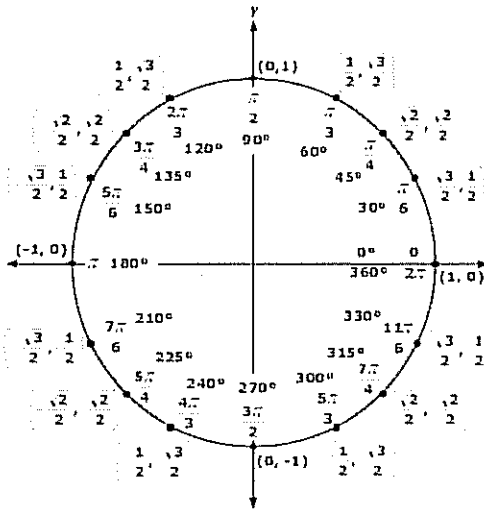
$$5. r\sqrt{a} + s\sqrt{a} = (r + s)\sqrt{a}$$

# TRIGONOMETRY

## Degrees and Radians

$$180^\circ = \pi$$

## The Unit Circle



$$P(\theta) = (\cos\theta, \sin\theta)$$

## Trigonometric Functions

$$F(x) = a \sin b(x - h) + k$$

OR

$$F(x) = a \cos b(x - h) + k$$

Amplitude:  $A = |a|$

$$\text{Period: } p = \frac{2\pi}{|b|}$$

Phase Shift:  $D = h$

Central Axis:  $y = k$

## Trigonometric Identities

$$\sin x = \frac{1}{\csc x} \quad \sec x = \frac{1}{\cos x}$$

$$\cos x = \frac{1}{\sec x} \quad \csc x = \frac{1}{\sin x}$$

$$\tan x = \frac{1}{\cot x} \quad \cot x = \frac{1}{\tan x}$$

$$\tan x = \frac{\sin x}{\cos x} \quad \cot x = \frac{\cos x}{\sin x}$$

$$\sin^2 x + \cos^2 x = 1$$

$$\tan^2 x + 1 = \sec^2 x$$

$$1 + \cot^2 x = \csc^2 x$$

$$\sin(A + B) = \sin A \cos B + \sin B \cos A$$

$$\sin(A - B) = \sin A \cos B - \sin B \cos A$$

$$\sin(2A) = 2 \sin A \cos A$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

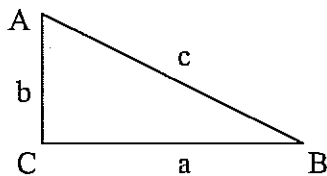
$$\cos(2A) = \cos^2 A - \sin^2 A$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$\tan(2A) = \frac{2 \tan A}{1 - \tan^2 A}$$

## Trigonometric Ratios



$$\sin B = \frac{\text{opp}}{\text{hyp}} = \frac{b}{c}$$

$$\sec B = \frac{\text{hyp}}{\text{adj}} = \frac{c}{a}$$

$$\cos B = \frac{\text{adj}}{\text{hyp}} = \frac{a}{c}$$

$$\csc B = \frac{\text{hyp}}{\text{opp}} = \frac{c}{b}$$

$$\tan B = \frac{\text{opp}}{\text{adj}} = \frac{b}{a}$$

$$\cot B = \frac{\text{adj}}{\text{opp}} = \frac{a}{b}$$